



ECE 3300 LAB 2 – Pre Lab

Transmission Lines and Time-domain Reflectometry

Overview: This document is a preparation for lab 2. It is due at the beginning of the lab session.

Equipment: Matlab® software is needed to complete this pre-lab.

For more information: Contact the teacher assistants or class instructor. See website for details: www.ece.utah.edu/~ece3300

Objectives:

- ◆ Learn about different types of transmission lines including coaxial cable, two wire lines, and microstrip.
- ◆ Measure the effect of external materials on capacitance and therefore impedance of a line.
- ◆ Understand the meaning of characteristic impedance Z_0 and how it differs from impedance $Z(z)$.
- ◆ Understand step function voltage transients on transmission lines.

Background:

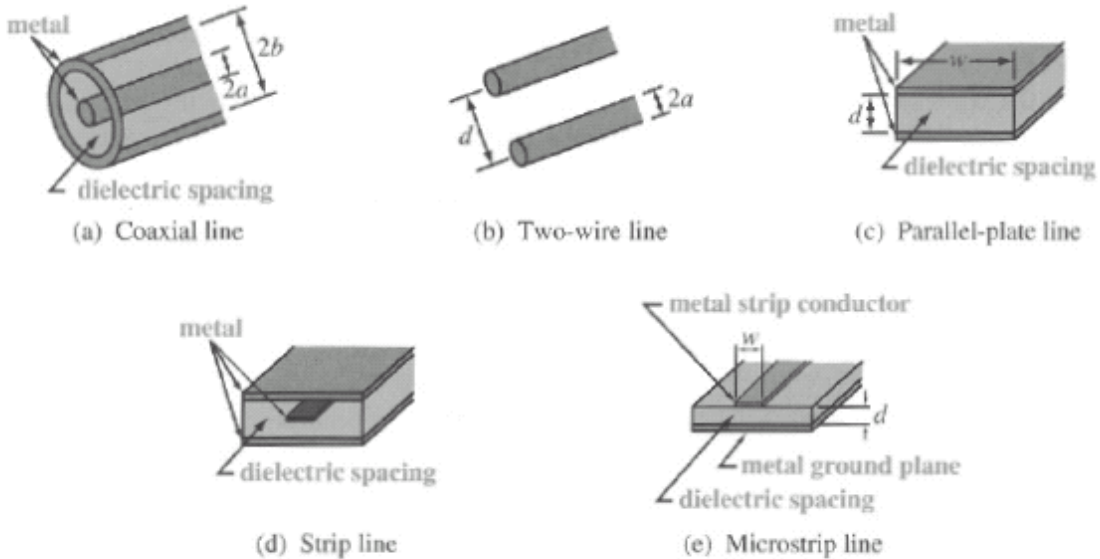
Students should understand before the lab:

- ◆ Lumped element (RLGC) model for transmission lines (TL) and how to calculate the RLGC parameters for a variety of transmission lines.
- ◆ How to make bounce diagrams and calculate the voltage at a point on the line as a function of time.

Pre-lab :

1. RLGC Model of Transmission Lines:

Write a Matlab™ code that will calculate the values of R, L, G, C, α , β , velocity of propagation, and Z_0 for a coaxial transmission line, two wire line, and parallel plate transmission line. The following information is from [1].



TEM Transmission Lines

Table 2-1: Transmission-line parameters R' , L' , G' , and C' for three types of lines.

Parameter	Coaxial	Two Wire	Parallel Plate	Unit
R'	$\frac{R_s}{2\pi} \left(\frac{1}{a} + \frac{1}{b} \right)$	$\frac{R_s}{\pi a}$	$\frac{2R_s}{w}$	Ω/m
L'	$\frac{\mu}{2\pi} \ln(b/a)$	$\frac{\mu}{\pi} \ln \left[(d/2a) + \sqrt{(d/2a)^2 - 1} \right]$	$\frac{\mu d}{w}$	H/m
G'	$\frac{2\pi\sigma}{\ln(b/a)}$	$\frac{\pi\sigma}{\ln \left[(d/2a) + \sqrt{(d/2a)^2 - 1} \right]}$	$\frac{\sigma w}{d}$	S/m
C'	$\frac{2\pi\epsilon}{\ln(b/a)}$	$\frac{\pi\epsilon}{\ln \left[(d/2a) + \sqrt{(d/2a)^2 - 1} \right]}$	$\frac{\epsilon w}{d}$	F/m

Notes: (1) Refer to Fig. 2-4 for definitions of dimensions. (2) μ , ϵ , and σ pertain to the insulating material between the conductors. (3) $R_s = \sqrt{\pi f \mu_c / \sigma_c}$. (4) μ_c and σ_c pertain to the conductors. (5) If $(d/2a)^2 \gg 1$, then $\ln \left[(d/2a) + \sqrt{(d/2a)^2 - 1} \right] \simeq \ln(d/a)$.

Test your code on the following transmission lines, and bring the code to lab with you:

RG58 Coaxial Line (cable type is printed on the side of the cable)

- ◆ The frequency is 1 GHz.
- ◆ The inner radius $a = 0.445$ mm, and the outer radius $b = 1.765$ mm.
- ◆ The conductor is copper ($\sigma_c = 5.8 \times 10^7$ S/m, $\mu_r = 1.0$).
- ◆ The insulation between the coaxial lines is polyethylene (PE) ($\epsilon_r = 2.25$, $\sigma = 0.0001$ S/m). Unless a material is clearly magnetic (ferrite materials), assume $\mu_r = 1.0$.

Answers for coax:

$$R = 3.6947 \text{ ohms/m}$$

$$L = 2.7557\text{e-}007 \text{ H/m}$$

$$G = 4.5602\text{e-}004 \text{ mohs/m}$$

$$C = 9.1164\text{e-}011 \text{ F/m}$$

$$\alpha = 0.0461 \text{ Np/m}$$

$$\beta = 31.4923 \text{ rad/m}$$

$$v_p = 1.9951\text{e+}008 \text{ m/s}$$

$$Z_o = 54.9796 - 0.0368i \text{ ohms}$$

Parallel Plate Line

- ◆ The frequency is 1 GHz.
- ◆ The polyethylene substrate has a thickness of 1mm.
- ◆ The top and bottom are made of copper.
- ◆ The width of the line is 6mm.

Twin Lead

- ◆ The frequency is 1 GHz.
- ◆ The radius of the wires is 2mm, and the distance between the wires is 6mm.
- ◆ Assume they are separated by polyethylene.

Answers for twin lead line:

$$R = 1.3131 \text{ ohms/m}$$

$$L = 3.8497\text{e-}007 \text{ H/m}$$

$$G = 3.2643\text{e-}004 \text{ mohs/m}$$

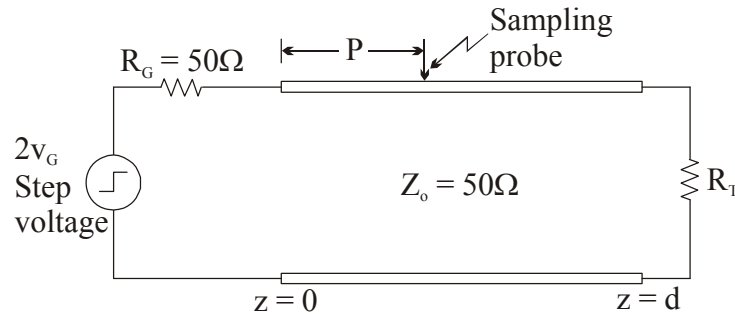
$$C = 6.5256\text{e-}011 \text{ F/m}$$

$$\alpha = 0.0211 \text{ Np/m}$$

$$\beta = 31.4923 \text{ rad/m}$$

$$v_p = 1.9951\text{e+}008 \text{ m/s}$$

$$Z_o = 76.8071 + 0.0097i \text{ ohms}$$

2. Voltage Step Function Response:

Sketch Voltage Reflection Diagrams (Bounce Diagrams) for a 50 Ω RG58 coaxial line connected to the following terminations. Assume $P = 1\text{m}$ and $d = 2\text{m}$. Use the velocity of propagation calculated in the previous section for polyethylene-filled coaxial line. Sketch the voltage at the sampling probe P as a function of time. Also calculate and show on your plot the steady state voltage (from Ulaby equation 2.159).

- Matched Load (50 Ω)
- Open Circuit
- Short Circuit
- Resistor = 100 Ω
- Resistor = 25 Ω
- 75 Ω transmission line that is 0.8 meters long and open at the end (connected to the 50 Ω line where R_T is shown). This creates tandem transmission lines, which are discussed in Agilent Application Note 1304-2.
- Inductor (qualitative drawing is sufficient), also discussed in the application note.
- Capacitor (qualitative drawing is sufficient), also discussed in the application note.

Questions:

- 2.1) Explain the concept of “step function response” of a system. See your circuits book if you do not remember.
- 2.2) Explain how the bounce diagrams and their related voltage vs. time plots relate to the step function response.

References

- [1] F. Ulaby, *Fundamentals of Applied Electromagnetics*, 6th ed., 2010, ch. 2.
- [2] Agilent Application Note 1304-2 on TDR Theory (available on the Lab website).
- [3] Step function response – see your basic circuits book.